Maths Calculation Policy

This policy supports the White Rose maths scheme used throughout the school. Progression within each area of calculation is in line with the programme of study in the 2014 National Curriculum. This calculation policy is used to support children to develop a deep understanding of number and calculation. This policy has been designed to teach children through the use of concrete, pictorial and abstract representations.

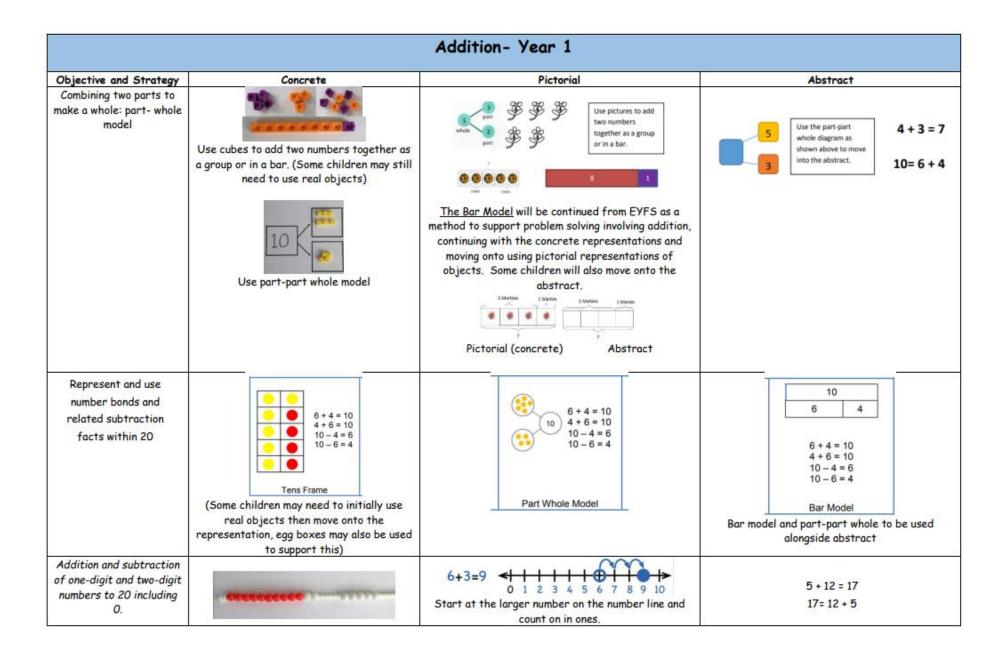
- Concrete representation— a pupil is first introduced to an idea or skill by acting it out with real objects. This is a 'hands on' component using real objects and is a foundation for conceptual understanding.
- Pictorial representation a pupil has sufficiently understood the 'hands on' experiences performed and can now relate them to representations, such as a diagram or picture of the problem.
- Abstract representation—a pupil is now capable of representing problems by using mathematical notation, for example 12 x 2 = 24. It is important that conceptual understanding, supported by the use of representation, is secure for all procedures. Reinforcement is achieved by going back and forth between these representations.

Mathematics Mastery

At the centre of the mastery approach is the belief that all children have the potential to succeed. They should have access to the same curriculum content and, rather than being extended with new learning, they should deepen their conceptual understanding by tackling challenging and varied problems. Similarly, with calculation strategies, children must not simply rote learn procedures but demonstrate their understanding of these procedures through the use of concrete materials and pictorial representations. This policy outlines the different calculation strategies that should be taught and used in EYFS to Year 6 in line with the requirements of the 2014 Primary National Curriculum.

This mathematics policy has been adapted from work by the NCETM. Teachers use a range of teaching resources and the policy does not recommend one set of resources over another, rather that, a variety of resources are used. For each of the four rules of number, different strategies are laid out, together with examples of what concrete materials can be used, along with suggested pictorial representations. The principle of the concrete-pictorial-abstract (CPA) approach is for children to have a true understanding of a mathematical concept they need to master all three phases within a year group's scheme of work.

Addition- EYFS Objectives Concrete Pictorial Abstract - Knows that a group of A focus on symbols things change in quantity and numbers to form when something is added. a calculation. Two groups of - Find the total number of pictures so children Use toys and general classroom resources for items in two groups by 5+2=7are able to count the counting all of them. children to physically manipulate, total. group/regroup. Aga Aga - Says the number that is one more than a given number. Use specific maths part resources such as 5 - Finds one more from a counters, snap group of up to five objects, cubes, Numicon Bar model using whole then ten objects. visuals, pictures/icons etc. 1 Marble or colours. - In practical activities and part discussion, beginning to use the vocabulary involved in adding. 2 3 4 5 Use visual supports - Using quantities and such as ten frames, 3 3 objects, they add two part part whole and single digit numbers and addition mats with count on to find the pictures/icons. answer. Use visual supports such as ten frames, part part - Solve problems including whole and addition mats, doubling. * No expectation for children to be with the physical objects able to record a number and resources that can be sentence/addition calculation. **:::** manipulated.



Start at the bigger number and counting on	Start with the larger number on the bead string and then count of to the smaller number 1 by 1 to find the answer.	12 + 5 = 17 Start at the larger number on the number line and count on in ones or in one jump to find the answer.	Place the larger number in your head and count on the smaller number to find your answer.
Regrouping to make 10 (The 'Make 10' strategy)	Start with the bigger number and use the smaller number to make 10. Use ten frames.	Use pictures or a number line. Regroup or Partition the smaller number using the part part whole model to make 10. 9 + 5 = 14	7 + 4= 11 If I am at seven, how many more do I need to make 10. How many more do I add on now?
Vocabulary	add, more, plus, and, make, alto	gether, total, equal to, equals, double, most, count on, nu	mber line, balancing, part, part, whole

Addition- Year 2			
Objective and Strategy Adding 3 1-digit numbers	Concrete 4 + 7 + 6= 17 Put 4 and 6 together to make 10. Add on 7. Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.	Pictorial Add together three groups of objects. Draw a picture to recombine the groups to make 10.	Abstract $4+7+6=10+7$ Combine the two numbers that make 10 and then add on the remainder.
Adding a 2-digit number and ones	Use ten frame to make 'magic ten Children explore the pattern. 17 + 5 = 22 27 + 5 = 32	Use partipart whole and number line to model. 17 + 5 = 22	17 + 5 = 22 Explore related facts 17 + 5 = 22 5 + 17 = 22 22
Adding a 2-digit number and multiples of 10	25 + 10 = 35 Explore that the ones digit does not change	27 + 30 +10 +10 +10 27 37 47 57 Base 10 may be used above the number line initially. The calculation will be shown alongside the number line to see the connection	27 + 10 = 37 27 + 20 = 47 27 + = 57

Adding two 2-digit numbers (No re-grouping)

24 + 15=

Add together the ones first then add the tens. Use the Base 10 blocks first before moving onto place value counters.

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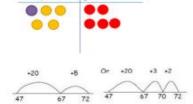
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(Some children may not be ready for place value counters in Y2)

Numicon may also be used



After practically using the base 10 blocks and place value counters, children can draw the counters to help them to solve additions.



Use number line and bridge ten using part whole if necessary.

Base 10 may be used above the number line.

The calculation will be shown alongside the number line to see the connection

Model	Calculation
	1

The Bar Model (Singapore maths) will be used to support problem solving moving onto the generalisation that b+c=a. Children will focus on using the abstract representation with the pictorial to support where necessary.

Partitioning:

Recording addition in columns supports place value and prepares for formal written methods with larger numbers.

Toward the end of the year, children move to more formal recording using partitioning method:

40 + 7 30 + 5 70 + 12

Vocabulary

add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, addition, column, tens boundary

	Add	lition- Year 3	
Objective and Strategy	Concrete	Pictorial	Abstract
Add and subtract numbers with up to 3-digits, using formal written methods of columnar addition Column addition (no regrouping)	Using manipulatives (dienes, numicon, counters), children are to line up hundreds, tens and ones. Children should be secure with using PV counters before moving onto pictorial. The calculation will be shown alongside the model used to see the connection	Children are to draw, in a PV frame, the manipulatives, that they are using. Secure knowledge of representation with the PV columns. The calculation will be shown alongside the model to see the connection Model Calculation	2 2 3 + 1 1 4 3 3 7 Children to move onto recording more formally. Some children may need to use the expanded method (see below).
Column addition (with regrouping)	Handreds Tens Ocean	Children can draw a representation of the grid to further support their understanding, carrying the ten underneath the line.	20 + 5 $40 + 8$ $60 + 13 = 73$ Children are to begin with the abstract expanded form. For those children, that are confident after AFL, the below method should be used.

	Exchange ten ones for a ten. Model using Dienes, Numicon and place value counters.	536 + 85 621 11
Vocabulary	addition add, more, and make, sum, total, altogether, double, near double, half, ha	The state of the s

	Add	lition- Year 4	
Objective and Strategy	Concrete	Pictorial	Abstract
Using formal written methods of columnar addition where appropriate add numbers with up to 4 digits (with exchange)	Children continue to use dienes or place value counters to add, exchanging ten ones for a ten and ten tens for a hundred and ten hundreds for a thousand.	Children can draw a pictoral representation of the columns and place	3517 + 396 3913 Continue from previous work to carry hundreds as well as tens.
	The calculation will be shown alongside the manipulative used to see the connection Model Calculation	value counters to further support their learning and understanding.	
Add decimals with 2 decimal places, including money.	Introduce decimal place value counters and model exchange for addition.	2.37 + 81.79 tens ones tends hundredes 00 0000 0 00000 000000 00 00000 0 00000	£23 · 59 + £7 · 55 €3 · 4 As the children move on, introduce decimals with the same number of decimal places and different. Money can be used
Vocabulary	addition add, more, and make, sum, total, altogether, d	ouble, near double, half, halve, tens boun	here. dary, hundreds boundary, decimal, decimal

Objective and Strategy	Concrete	Pictorial	Abstract
add numbers with more than 4 digits.	See Year 4	See Year 4	Children should have abstract supported by a pictorial or concrete if needed.
add several numbers of increasing complexity, including adding money, measure and decimals with different numbers of decimal points.	See Year 4	See Year 4	8 1,05 9 3,66 8 15,30 1 + 20,551 1 20,579 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
/ocabulary	addition add, more, and make, sum, total, alto	ether, double, near double, half, halve decimal point	e, tens boundary, hundreds boundary, decimal,

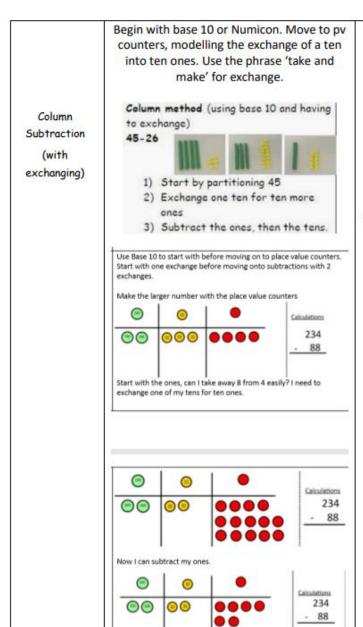
Subtraction- EYFS Objectives Concrete Pictorial Abstract - Knows that a group of A focus on symbols things change in quantity and numbers to form when something is taken a calculation. away 10 - 1 = ?- Find one less from a Use toys and general classroom resources for group of five objects, then children to physically manipulate, ten objects. group/regroup. - In practical activities and discussion, beginning to use the vocabulary involved in subtracting. - Using quantities and A group of pictures for children to cross out 3 objects, they subtract two or cover quantities to support subtraction. single digit numbers and count back to find the answer. 7 - 3 = ?Use specific maths resources such as snap cubes, Numicon, bead strings etc. * No expectation for children to be able to record a number Use visual supports such as ten frames, part sentence/addition calculation. Use visual supports such as ten frames, part part part whole and bar model with pictures/icons. whole and subtraction mats, with the physical objects and resources that can be manipulated.

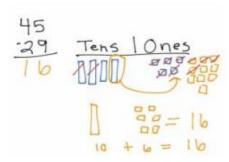
Subtraction- Year 1			
Objective and Strategy	Concrete	Pictorial	Abstract
Subtract one-digit and two-digit numbers to 20, including 0. Taking away ones	Use physical objects, counters, cubes etc to show how objects can be taken away. $6-4=2$ $4-2=2$	Cross out drawn objects to show what has been taken away.	7—4 = 3 16—9 = 7
Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones. 13 - 4 Use counters and move them away from the group as you take ther away counting backwards as you go.	Count back on a number line or track Start at the bigger number and count back the smaller number showing the jumps on the number line.	Put 13 in your head, count back 4. What number are you at? (Use your fingers to help you)

Find the difference	Compare objects and amounts 7 'Seven is 3 more than four' 4 'I om 2 years older than my sister' 5 Pench 2 Lay objects to represent bar model.	Count on to find the difference. 1 2 3 4 5 6 7 8 9 10 11 12 Comparison Bar Models Draw bars to find the difference in oge between them. 13 7 Line 3 line 22	Hannah has12 sweets and her sister has 5. How many more does Hannah have than her sister?
Represent and use number bonds and related subtraction facts within 20 Part-part whole model	Unk to addition. Use PPW model to model the inverse. If 10 is the whole and 6 is one of the arts, what 5 the other part? 10—6 = 4	Use a pictorial representation of objects to show the part-part whole model	Move to using numbers within the part whole model.
Make 10	Make 14 on the ten frame. Take away the four first to make 10 and then takeaway one more so you have taken away 5. You are left with the answer of 9.	13 - 7 = 6 3 4 Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.	16 – 8= How many do we take off to reach the next 10? How many do we have left to take off?
Vocabulary	equal to, take, take-away, less, minus, subtract, leaves, many left, how much less is	distance between, how many more, how many fewer/	less than, most, least count back, how

Subtraction- Year 2				
Objective and Strategy	Concrete	Pictorial	Abstract	
Subtract a two-digit number and ones, a two- digit number and tens, two two-digit numbers Partitioning to subtract without re- Grouping: 'Friendly numbers'	Use Dienes to show how to partition the number when subtracting without regrouping. The calculation will be shown alongside the manipulative used Model Calculation	Children draw representations of Dienes and cross off. 43—21 = 22	Recording subtraction in columns supports place value and prepares for formal written methods with larger numbers. Toward the end of the year, children move to more formal recording using partitioning method: e.g. 43-21=22 40 and 3 -20 and 1 20 and 2	
Make ten strategy	34—28 Use a bead bar or bead strings to model counting to next ten and the rest.	76 80 90 93 'counting on' to find 'difference' Use a number line to count on to next ten and then the rest.	93—76 = 17	
Vocabulary	equal to, take, take-away, less, minus, subtract, leaves, d	istance between, how many more, how many fewer/ s isdifference, count on, strategy, partition, tens		

Subtraction- Year 3				
Objective and Strategy	Concrete	Pictorial	Abstract	
To subtract numbers with up to three-digits, using formal written	subtract pers with up pree-digits, ing formal Children are to be secure with use of PV counters before moving onto abstract.		Children should begin with the expanded form. Movin onto a more formal way as below.	
methods of columnar subtraction	11: -	© © Calculations 176 - 64 = 176 - 64 112	$47 - 24 = 23$ $-\frac{40 + 7}{20 + 3}$ $728 - 582 = 146$ $7 = 2$ $7 = 2$ $7 = 2$ $7 = 3$	
Column subtraction (without exchanging)	Use base 10 or Numicon to model The calculation will be shown alongside the model chosen to see the connection Model Calculation			



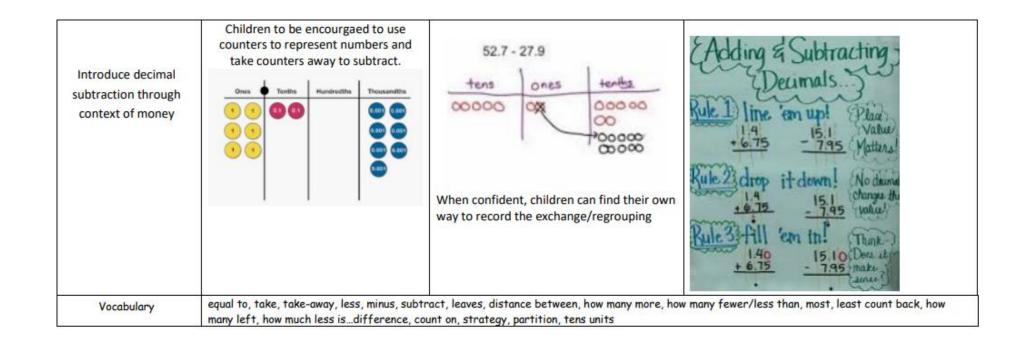


When confident, children can find their own way to record the exchange/regrouping

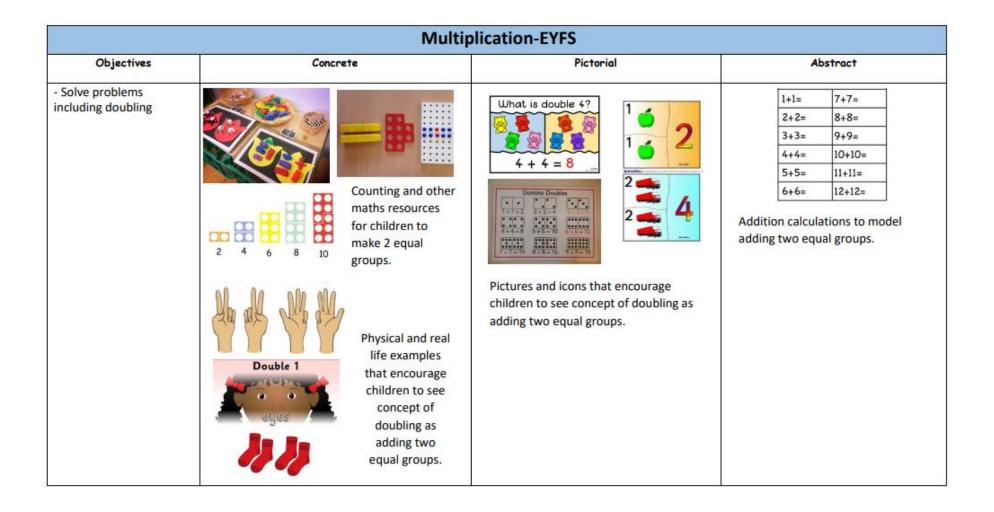
Children should begin with the expanded form. Moving onto a more foraml way as below (bottom picture).

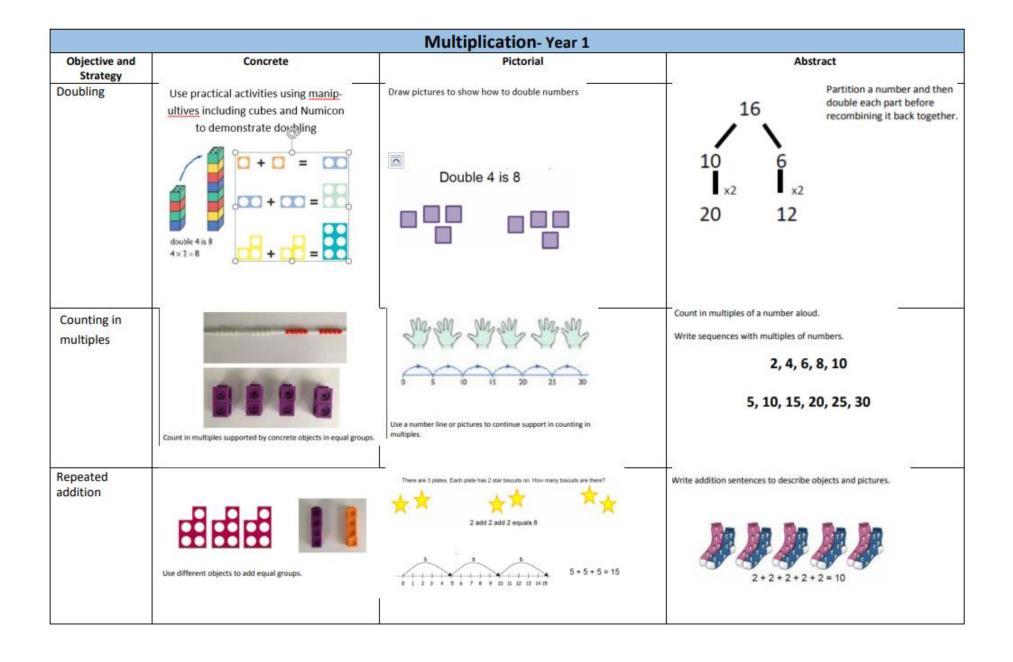


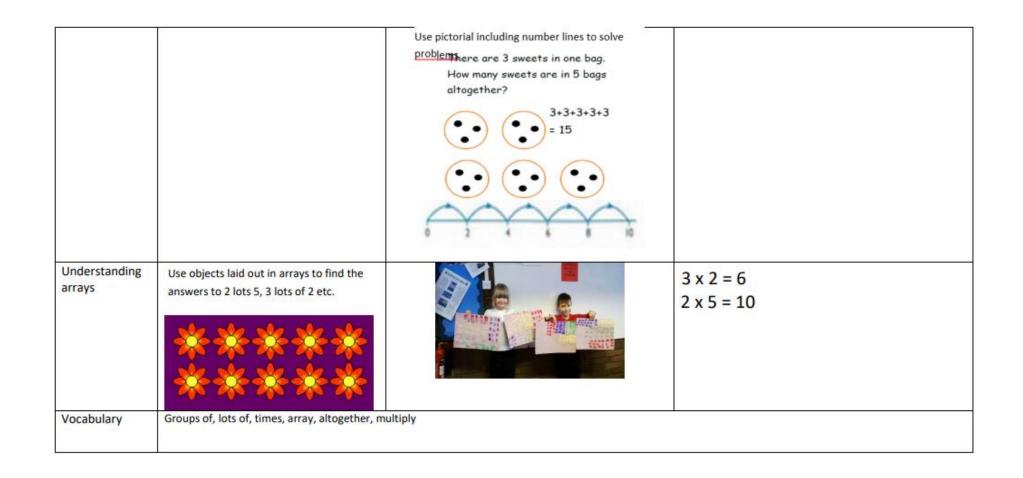
Now look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens. Calculations 234 - 88 Now I can take away eight tens and complete my subtraction 1234 88 146 Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount. equal to, take, take-away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least count back, how many left, Vocabulary how much less is ... difference, count on, strategy, partition, tens units Subtraction- Year 4 Objective and Strategy Concrete Pictorial Abstract Subtract numbers with Children to draw pv counters and show up to 4 digits using the their exchange—see Y3 formal written methods The calculation will be shown alongside the appropriate of columnar model chosen to see the connection Model process of exchange using subtraction where appropriate Numicon, base ten and then move to Model Calculation PV counters. Year 4 subtractraction Use the phrase 'take and make' for with up to 4 digits. exchange- see Y3 The calculation will be shown alongside the model chosen to see the connection This will lead to an understanding of subtracting any number including decimals. Calculation Model



Subtraction- Year 5/6			
Objective and Strategy	Concrete	Pictorial	Abstract
Subtract with at least 4 digits, including money and measures. Subtract with increasingly large and more complex numbers and decimal values (up to 3 decimal place).	See Year 4	See Year 4	"X" 8 16, 6 9 9 - 89, 9 4 9 - 60, 7 5 0 "Y 10 5 · 34 1 9 kg - 36 · 08 0 kg - 3 6 · 0 8 0 kg
Vocabulary	equal to, take, take-away, less, minus, subtract, leaves, dist left, how much less isdifference, count on, strategy, part	-	any fewer/less than, most, least count back, how many

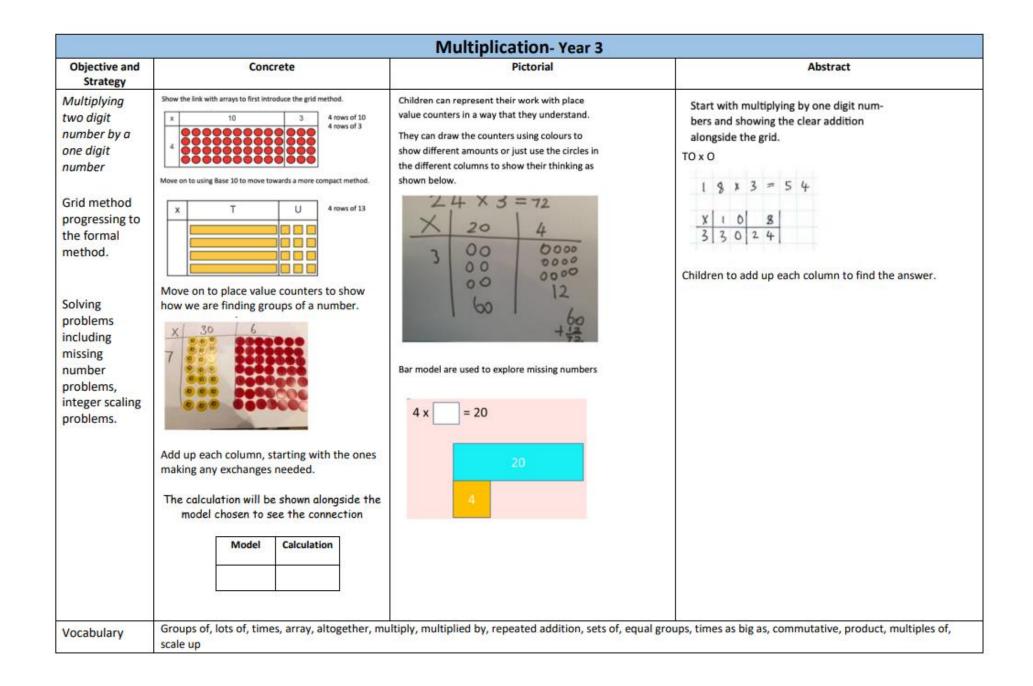


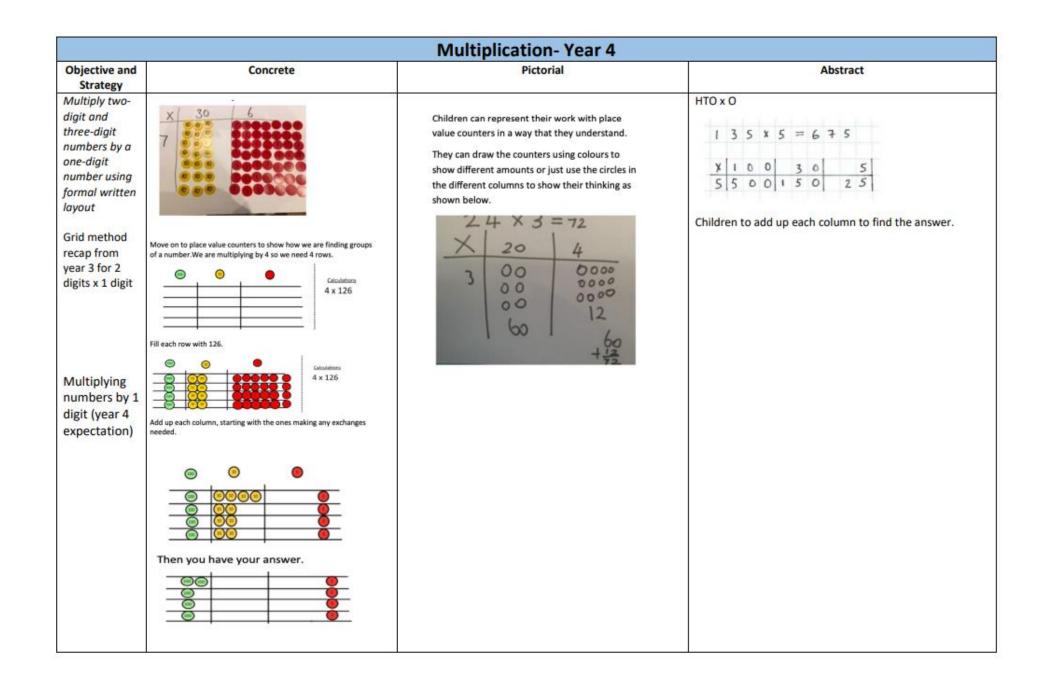


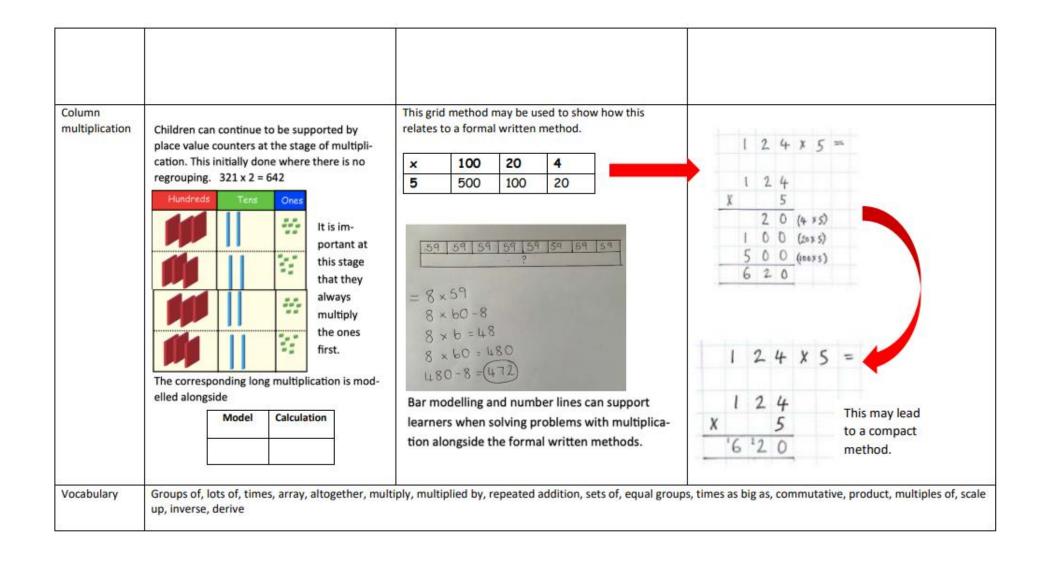


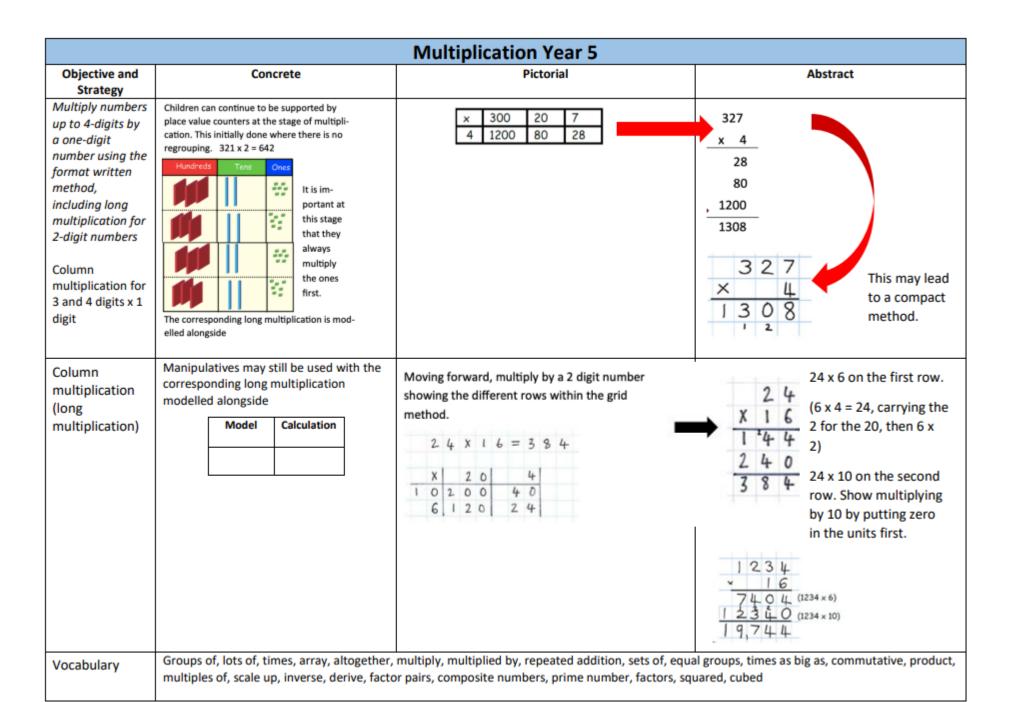
		Multiplication- Year 2	
Objective and Strategy	Concrete	Pictorial	Abstract
Counting in multiples of 2, 3, 4, 5, 10 from 0 (repeated addition)	Count the groups as children are skip counting, children may use their fingers as they are skip counting. Use bar models. 5+5+5+5+5+5+5+5+5=40	Number lines, counting sticks and bar models should be used to show representation of counting in multiples. 3 3 3 3 3	Count in multiples of a number aloud. Write sequences with multiples of numbers. 0, 2, 4, 6, 8, 10 0, 3, 6, 9, 12, 15 0, 5, 10, 15, 20, 25, 30
Multiplication is commutative	Create arrays using counters and cubes and Numicon. Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.	Use representations of arrays to show different calculations and explore commutativity.	12 = 3 × 4 12 = 4 × 3 Use an array to write multiplication sentences and reinforce repeated addition. 5 + 5 + 5 = 15 3 + 3 + 3 + 3 + 3 = 15 5 x 3 = 15 3 x 5 = 15

sing the	8	2 x 4 = 8
verse		4 x 2 = 8
nis should	4 2	8 + 2 = 4
		8 ÷ 4 = 2
ught	× =	8 = 2 x 4
ongside	× =	8 = 4 x 2
vision, so	$\square \div \square = \square$	2 = 8 + 4
arn how		4 = 8 ÷ 2
ork ongside ach other.		Show all 8 related fact family sentences.
ocabulary Groups of, lots of, time	s, array, altogether, multiply, multiplied by, repeated ac	dition, sets of, equal groups, times as big as, commutative.





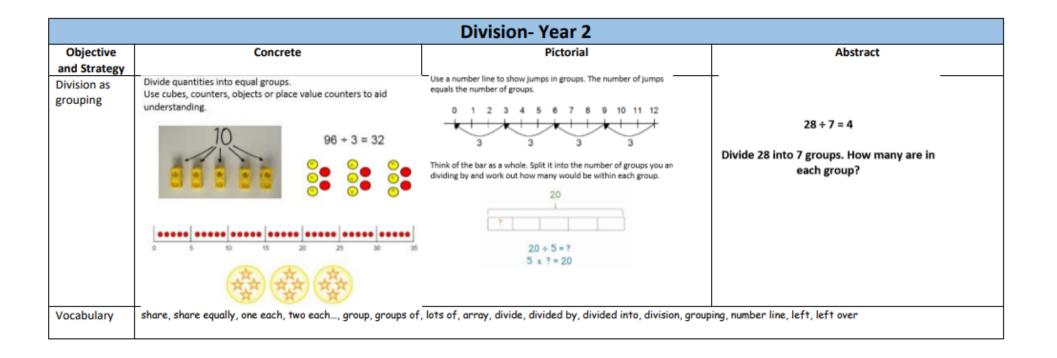




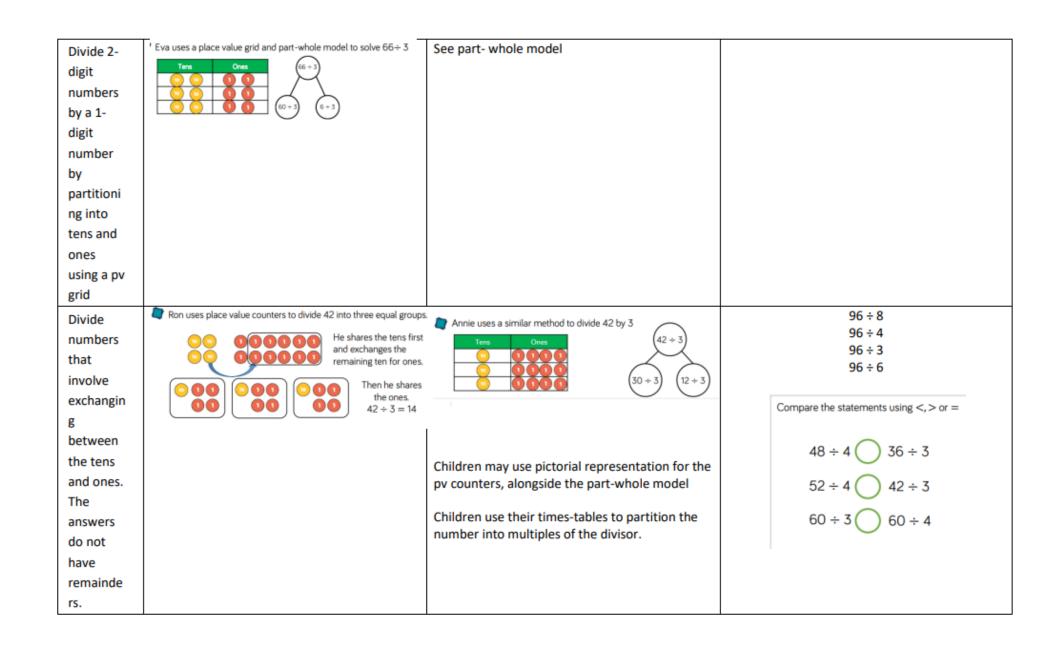
	Multiplication- Year 6			
Objective and Strategy	Concrete	Pictorial	Abstract	
Multiply decimal up to 2 decimal place by a single digit.			Remind children that the single digit belongs in the units column. Line up the decimal points in the question and the answer. 3 • 1 9 × 8 2 5 • 5 2	
vocabulary		multiply, multiplied by, repeated addition, sets of, equal r pairs, composite numbers, prime number, factors, squa		

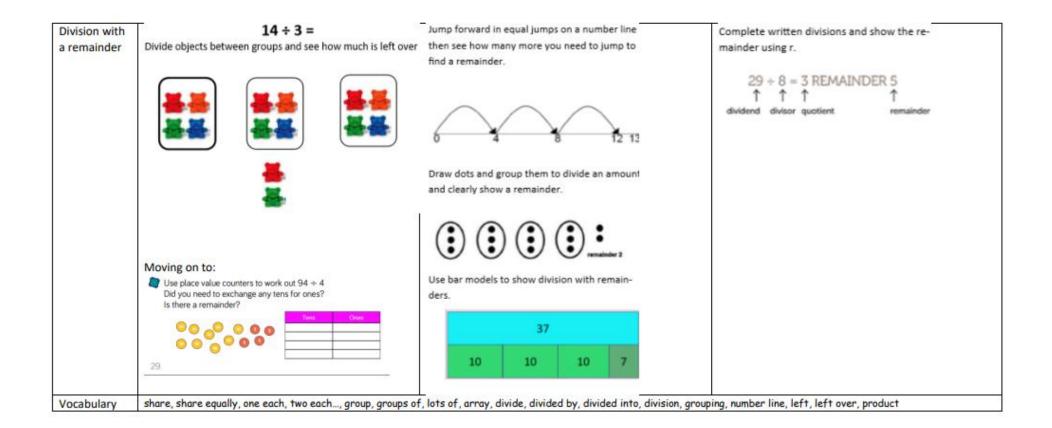
Division- EYFS			
Objectives	Concrete	Pictorial	Abstract
Halving a whole, halving a quantity of objects. Sharing a quantity of output outp		☆ I	
objects.	Children have the opportunity to physically cut objects, food or shapes in half. Counting and other maths resources for children to share into two equal groups. Use visual supports such as halving mats and part part	Pictures and icons that encourage children to see concept of halving in relation to subitising, addition and subtraction knowledge. i.e. Knowing 4 is made of 2 groups of 2, so half of 4 is 2. Bar model with pictures or icons to support understanding of finding 2 equal	
	whole, with the physical objects and resources that can be manipulated. Counting and other maths resources for children to explore sharing between 3 or more.	parts of a number, to further understand how two halves make a whole. Pictures for children to create and visualise 3 or more equal groups.	

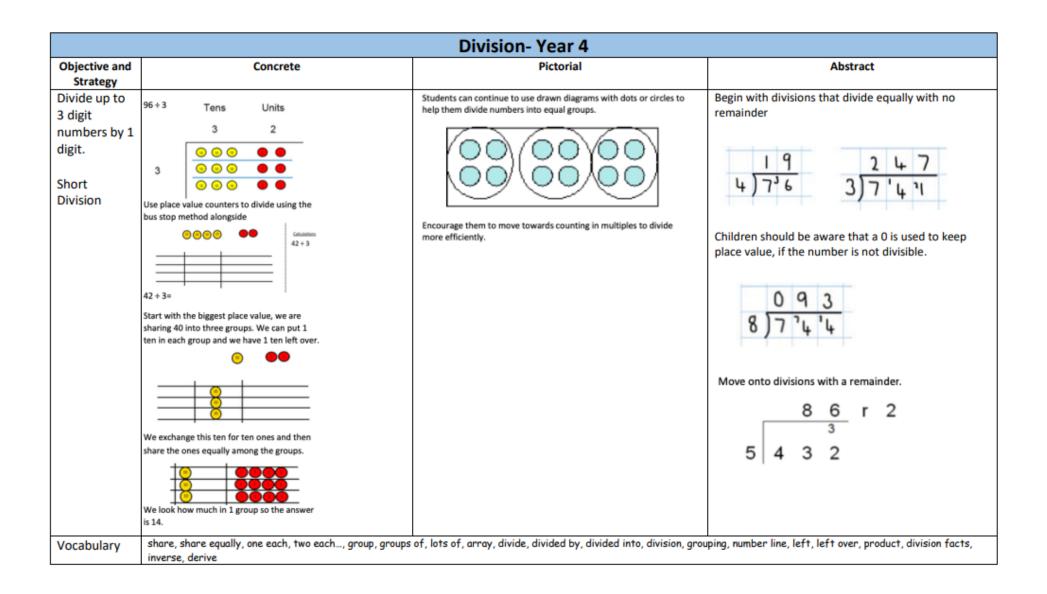
		Division- Year 1	
Objective and Strategy	Concrete	Pictorial	Abstract
Division as sharing (sharing objects into groups)	I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quantities. $8 \div 2 = 4$ Children use bar modelling to show and support understanding.	Share 9 buns between three people. 9 ÷ 3 = 3
		12	
		000 000 000 000	
50		12 ÷ 4 = 3	0
Vocabulary s	share, share equally, one each, two each, group, groups	of, lots of, array	

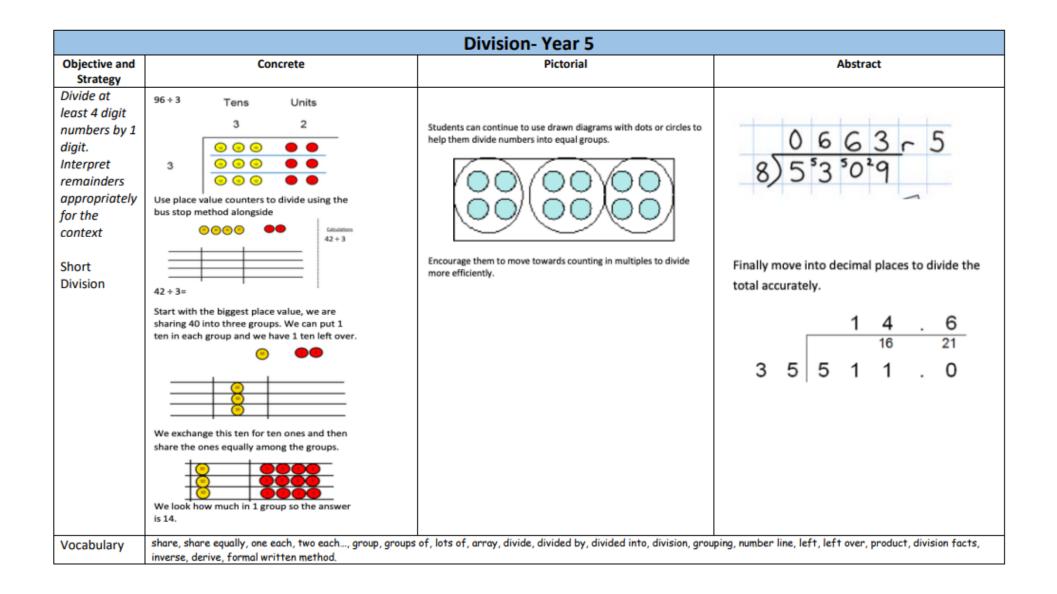


Objective and Strategy	Concrete	Pictorial	Abstract
Division as grouping	Use cubes, counters, objects or place value counters to aid understanding.	Continue to use bar modelling to aid solving division problems.	How many groups of 6 in 24?
		?	24 ÷ 6 = 4
	24 divided into groups of 6 = 4 96 + 3 = 32	20 ÷ 5 = ? 5 x ? = 20	
Division with arrays		Draw an array and use lines to split the array into groups to make multiplication and division sentences	Find the inverse of multiplication and division sentences by creating eight linking number sentences. 7 x 4 = 28
	Link division to multiplication by creating an	0 0 0 0	4 x 7 = 28
	array and thinking about the number sentenc- es that can be created.	00000	28 ÷ 7 = 4 28 ÷ 4 = 7
	Eg 15 ÷ 3 = 5 5 x 3 = 15	00000	28 = 7 x 4
	15 ÷ 5 = 3 3 x 5 = 15		28 = 4 x 7 4 = 28 ÷ 7
			7 = 28 ÷ 4









	Division-Year 6
Objective and Strategy	Abstract
Long Division	Step 1 – a remainder in the ones
	0 4 1 R1 4) 16 5
	4 does not go into 1 (hundred). So combine the 1 hundred with the 6 tens (160).
	4 goes into 16 four times.
	4 goes into 5 once, leaving a remainder of 1.
	8) 3207
	8 does not go into 3 of the thousands. So combine the 3 thousands with the 2 hundreds (3,200).
	8 goes into 32 four times (3,200 + 8 = 400) 8 goes into 0 zero times (tens). 8 goes into 7 zero times, and leaves a remainder of 7.
	0 6 1 4) 2 4 7 -4 3
	When dividing the ones, 4 goes into 7 one time. Multiply 1 × 4 = 4, write that four under the 7, and subract. This finds us the remainder of 3.
	Check: 4 × 61 + 3 = 247
	th h t o 0402 4) 1609 -8 1
	When dividing the ones, 4 goes into 9 two times. Multiply 2 × 4 = 8, write that eight under the 9, and subract. This finds us the remainder of 1.
	Check: 4 × 402 + 1 = 1,609
	Step 2 – a remainder in the tens

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
2 2)58	2 2)58 -4 1	2 9 2) 5 8 -4 1 1 8
Two goes into 5 two times, or 5 tens + 2 = 2 whole tens but there is a remainder!	To find it, multiply 2 × 2 = 4, write that 4 under the five, and subtract to find the remainder of 1 ten.	Next, drop down the 8 of the ones next to the leftover 1 ten. You combine the remainder ten with 8 ones, and get 18.

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
2 9 2) 5 8 -4 1 8	2 9 2) 5 8 -4 1 8	2 9 2) 5 8 -4 1 8
Divide 2 into 18. Place 9 into the quotient.	Multiply 9 × 2 = 18, write that 18 under the 18, and subtract.	- 1 8 0 The division is over since there are no more digits in the dividend. The quotient is 29.

Step 3 - a remainder in any of the place values

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
h t o	hto	h t o 1 8
2)278	2)278	2)278
	<u>-2</u> 0	-2 1 0 7
Two goes into 2 one time, or 2 hundreds + 2 = 1 hundred.	Multiply 1 × 2 = 2, write that 2 under the two, and subtract to find the remainder of zero.	Next, drop down the 7 of the tens next to the zero.
Divide.	Multiply & subtract.	Drop down the next digit.
h t o	h t o	hto
1 3 2)278	2)278	2)278
<u>-2</u>	- <u>2</u>	<u>-2</u> 07
	- 6	- 6
Divide 2 into 7. Place 3 into the quotient.	Multiply 3 × 2 = 6, write that 6 under the 7, and subtract to find the remainder of 1 ten.	Next, drop down the 8 of the ones next to the 1 leftover ten.
1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
h t o	hto	hto
13 <mark>9</mark> 2)278	2)278	2)278
$\frac{-2}{0.7}$	- <u>2</u>	- <u>2</u>
- 6	- 6	- <u>6</u> 18
10	-18 0	<u>-18</u>
Divide 2 into 18. Place 9 into the quotient.	Multiply 9 × 2 = 18, write that 18 under the 18, and subtract to find the remainder of zero.	There are no more digits to drop down. The quotient is 139.

Vocabulary

share, share equally, one each, two each..., group, groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, product, division facts, inverse, derive, formal written method.